## SINGULAR AND DOUBLE-PHASE PROBLEMS: NEW RESULTS AND SOME PERSPECTIVES

## VICENŢIU D. RĂDULESCU

In this talk, I shall report on some joint works in collaboration with P. Pucci (Perugia), N. Papageorgiou (Athens) and D. Repovs (Ljubljana). I shall be concerned with several types of singular or multi-phase phenomena arising in the theory of nonlinear elliptic equations. I will describe some striking results related to the existence of blow-boundary solutions, the generalized maximum principle, and a discontinuity property of the spectrum for double-phase problems. We establish that no monotonicity hypotheses are necessary in the statement of some classical theorems. Several open problems are raised in the final part of this lecture.

Department of Mathematics,

UNIVERSITY OF CRAIOVA AND INSTITUTE OF MATHEMATICS OF THE ROMANIAN ACADEMY, BUCHAREST *E-mail address:* radulescu@inf.ucv.ro